

1) b) find $A + \phi_0$

$$\underline{A} = -10\text{ cm} + i 2\text{ cm}$$

$$A = \sqrt{(A_R)^2 + (A_I)^2} = \sqrt{(-10\text{ cm})^2 + (2\text{ cm})^2} = \boxed{\sqrt{104}\text{ cm}}$$

$$\phi_0 = \tan^{-1}\left(\frac{A_I}{A_R}\right) = \tan^{-1}\left(\frac{2\text{ cm}}{10\text{ cm}}\right) = \boxed{-11.3^\circ \text{ or } -1.97\text{ rad}}$$

2) a) start with $x(t) = x_{eq} + A \cos(\omega_0 t + \phi_0)$

given Euler's Identity $e^{i\theta} = \cos\theta + i\sin\theta$

$$x(t) = x_{eq} + \text{Re} \left[A e^{i(\omega_0 t + \phi_0)} \right]$$

substitute $\underline{A}$ in for $A e^{i\phi_0}$

$$x(t) = x_{eq} + \text{Re} \left[\underline{A} e^{i\omega_0 t} \right]$$

Given that any complex number $\underline{B}$ can be written as $B_R + iB_I$ and has a complex conjugate

$\underline{B}^* = B_R - iB_I$ It is true that

$$\underline{B} + \underline{B}^* = B_R + iB_I + B_R - iB_I = 2B_R$$

$$\text{or } \frac{1}{2} [\underline{B} + \underline{B}^*] = \text{Re}[\underline{B}]$$

$$\therefore x(t) = x_{eq} + \frac{1}{2} \left[\underline{A} e^{i\omega_0 t} + \underline{A}^* e^{-i\omega_0 t} \right]$$