

$$\Rightarrow -10\underline{A} + 25.5i\underline{A} + 6 \times 10^{-2} + 10\underline{A} + .153i + 25.5i\underline{A} = -.16$$

$$\underline{A}(-10 + 25.5i + 10 + 25.5i) = -.16 - 6 \times 10^{-2} - .153i$$

$$\underline{A}(51i) = -.22 - .153i$$

$$\underline{A} = \frac{-.22 - .153i}{51i} = +.0043i - .003$$

$$\underline{B} = -6 \times 10^{-3} - \underline{A} = -6 \times 10^{-3} + .0043i + .003 = -.003 - .0043i = \underline{A}^*$$

particular solution is:

$$X(t) = X_{eq} + (.0043i - .003)e^{(-10 + 25.5i)t} + (-.003 - .0043i)e^{(-10 - 25.5i)t}$$

NOTE THAT, EVEN THOUGH EACH OF THE EXPONENTIAL TERMS IN THE ABOVE EQUATION IS COMPLEX, $X(t)$ is REAL because they are COMPLEX CONJUGATE of each other.

Using arguments similar to the ones in Pr. 2(a), we can cast this in a form similar to the solution to PS#1, Pr. 3(b):

$$X(t) = X_{eq} + e^{-bt/2} [\underline{A}e^{i\omega't} + \underline{A}^*e^{-i\omega't}]$$

$$(\text{with } \underline{A} = (-0.003 + i0.0043)m, \quad b = 20s^{-1},$$

$$\omega' = \sqrt{\omega_0^2 - b^2/4} = 25.5s^{-1})$$

$$= X_{eq} + 2Ae^{-bt/2} \cos(\omega't + \phi_0) \quad (\text{with } \underline{A} = Ae^{i\phi_0})$$

$$= \underline{X_{eq} + 2Ae^{-bt/2} \sin(\omega't + \phi_0 - \frac{\pi}{2})} \quad \left\| \begin{array}{l} A = \sqrt{(0.003)^2 + (0.0043)^2} m \\ \tan \phi_0 = \frac{0.0043}{-0.003} \end{array} \right.$$