

$$b) A = \frac{F_0/m}{|\omega_0^2 - \omega^2 + c\omega^4|} \Rightarrow \frac{A}{f} = \frac{A}{(F_0/m)} = \frac{1}{|\omega_0^2 + c\omega^4 - \omega^2|}$$

In the limits  $\omega \rightarrow 0$  and  $\omega \rightarrow \infty$ , we get respectively:

$$1) \omega \rightarrow 0: \left(\frac{A}{f}\right)(\omega=0) = \frac{1}{\omega_0^2}$$

$$2) \omega \rightarrow \infty: \left(\frac{A}{f}\right)(\omega \rightarrow \infty) = 0$$

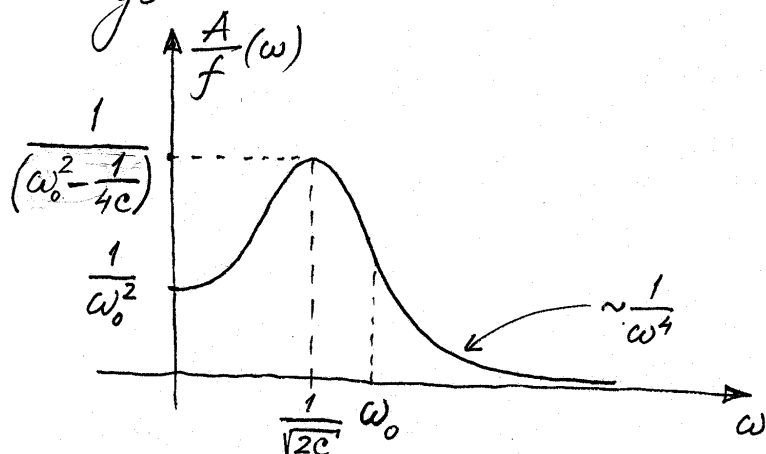
To understand the behavior in between, we have to study where the denominator of  $A/f$  has zeroes:

$$c\omega^4 - \omega^2 + \omega_0^2 = 0 \Rightarrow \omega = \pm \sqrt{\frac{1 \pm \sqrt{1 - 4c\omega_0^2}}{2c}}$$

We see that there are 2 DISTINCT CASES:

$$\boxed{\text{I.}} \quad \underline{c > \frac{1}{4\omega_0^2} :}$$

The function  $c\omega^4 - \omega^2 + \omega_0^2$  has NO REAL ZEROES; therefore,  $A/f(\omega)$  has NO POLES. For positive  $\omega$ 's we get:



$$\underline{\varphi(\omega) \equiv 0}$$

for ALL  $\omega$ 's.