

⑤

Next, let us evaluate $(A/f)(\omega)$ at $\omega = \omega_0$, $\omega_{1,2} = \omega_0 \pm \frac{b}{2}$ in this limit. Keeping the lowest non-vanishing order in b , we get:

$$\begin{aligned} \bullet (A/f)(\omega = \omega_0) &= \frac{1}{\sqrt{(\omega_0^2 - \omega_0^2)^2 + (b\omega_0)^2}} = \frac{1}{\underline{b\omega_0}} \\ &= \underline{(A/f)_{\max}} \end{aligned}$$

$$\begin{aligned} \bullet (A/f)(\omega = \omega_1) &= \frac{1}{\sqrt{(\omega_0^2 - \omega_1^2)^2 + (b\omega_1)^2}} \\ &= \frac{1}{\sqrt{[\omega_0^2 - (\omega_0 + \frac{b}{2})^2]^2 + b^2(\omega_0 + \frac{b}{2})^2}} \\ &= \frac{1}{\sqrt{(\cancel{\omega_0^2} - \cancel{\omega_0^2} - b\omega_0 - \frac{b^2}{4})^2 + b^2\omega_0^2 + \frac{b^4}{2}}} \\ &= \frac{1}{\sqrt{b^2\omega_0^2 + b^2\omega_0^2}} = \frac{1}{\underline{\sqrt{2} b\omega_0}} = (A/f)(\omega = \omega_2) \end{aligned}$$

[In the above calculation, we used $\underline{b^2 \ll b\omega_0}$ and $\underline{b^4 \ll b^2\omega_0^2}$, which follow directly from $\underline{b \ll \omega_0}$.]